Abstract—The performance increase up to the sensor resolution in repetitive control (RC) invalidates the standard assumption in RC that data is available at equidistant time instances, e.g., in systems with package loss or when exploiting timestamped data from optical encoders. The aim of this paper is to develop an intermittent sampling RC framework for non-equidistant measurements. Sufficient stability conditions are derived that can be verified using non-parametric frequency response function data. This results in a frequency domain design procedure to explicitly address uncertainty. The RC framework is validated on an industrial printbelt setup for which exact non-equidistant measurement data is available.

I. INTRODUCTION

Learning control methods, including repetitive control (RC) [1] and iterative learning control (ILC) [2], can achieve major performance improvements up to the sensor resolution for periodic tasks [3], [4]. RC and ILC are based on the internal model principle (IMP) [5], in which the key idea is to iteratively adjust the input based on errors from the previous executions of the same task by including a model of the disturbance in the controller. The main difference between ILC and RC is that the final state of the current task is carried over to the initial state of the next task in RC. For ILC, the state is reset after each task to the same initial condition.

Successful RC methods typically rely on 1) a stability test that can be verified using non-parametric models in the form of identified frequency response function (FRF) data and 2) an intuitive frequency domain design framework based on loop-shaping to explicitly address uncertainty [6], [7]. A common approach is based on a buffer in positive feedback interconnection with itself [8], [9], complemented by a learning and robustness filter, with possible extensions to uncertain period times [10], [11] and multiple periods [12], [13]. Further refinements include basis functions in the form of parallel periodic signal generators [14]. These frameworks rest on the assumption that exact data is available at all samples, allowing for linear time-invariant (LTI) stability and design frameworks such as Nyquist and Bode diagrams.

The assumption in RC that exact measurement data is available equidistantly in time, i.e., at all sample instances, is not always valid. For example, encoders sampled at an equidistant rate result in quantization errors. However, they are exact at the timestamp of the measurement [15]. Package loss in networked control systems similarly results in intermittently sampled measurements. In low-performance feedback control, intermittent sampling effects and resulting quantization can be neglected as they are insignificant compared to the magnitude of the converged error. Due to the increased performance up to the sensor resolution in RC, these effects are no longer negligible and, if left unaddressed, deteriorate performance.

Non-equidistant measurement data is addressed in ILC through combining the IMP with a worst-case analysis for arbitrary time-varying measurement points. Alternatively, the availability of data at each time instant is modelled as a known probability distribution in [16], [17]. This probability distribution is unknown in many applications, thus, a worst-case analysis is preferred. However, none of these methods can straightforwardly be extended to RC due to the state-reset in ILC that is not present in RC, necessitating an infinite-time instead of finite-time analysis.

Although RC has been substantially developed for a large range of practical problems, at present an RC approach that can deal with intermittent measurement, as occurring in, e.g., encoders or networked control systems, is not yet available. The aim of this paper is to design an RC framework that can asymptotically reject periodic disturbances when measurement data is available at non-equidistant samples.

The main contribution of this paper is an intermittent sampling RC framework that employs intermittent data for asymptotically rejecting periodic disturbances that can be successfully implemented in practice. This is achieved through the following sub-contributions.

C1 Stability tests for any realization of the measurement data, based on (identified) FRF data (Section III).
C2 Design guidelines through loop-shaping techniques to explicitly address uncertainty (Section IV).
C3 Experimental validation of the developed framework on an industrial printbelt setup (Section V).

Notation and Definitions

All systems are discrete-time, single-input single-output (SISO) and linear with sample rate $T_s$. The set of real rational, SISO, proper, asymptotically input-output stable, discrete-time transfer functions is denoted by $\mathcal{RH}_\infty$. The sets $\mathbb{N}$ and $\mathbb{Z}$ indicate the set of all positive integers, and the set of all integers, respectively. The $\ell_2$-norm of an infinite sequence of scalars $y = (\ldots, y(-2), y(1), y(0), y(1), y(2), \ldots)$, $y(k) \in \mathbb{R}$, $k \in \mathbb{Z}$, is defined as $\|y\|_{\ell_2} = \left(\sum_{k=-\infty}^{\infty} |y(k)|^2 \right)^{\frac{1}{2}}$. The space $\ell_2$
consists of all infinite sequences with finite $\ell_2$-norm.

II. Problem Formulation

In this section, the problem of intermittent sampling RC is introduced. First, traditional RC is presented. Second, the concept of timestamped data is introduced and combined with the traditional RC setup. Lastly, the problem is posed.

A. Repetitive Control

RC is a feedback control method to asymptotically reject periodic disturbances acting on a dynamic process. Consider the repetitive control setup in Fig. 1 (left). The goal of RC is to reject the influence of the periodic disturbance $v(k) \in \mathbb{R}$ on the error $e(k) \in \mathbb{R}$ given by

$$e(k) = y(k) + v(k), \quad (1)$$

where $y(k) \in \mathbb{R}$ is the output of dynamic process $J$, i.e.,

$$y(k) = J u(k). \quad (2)$$

Here $u(k) \in \mathbb{R}$ is the input to the process, and $k \in \mathbb{Z}$ the discrete timestep. $J$ can represent either a closed-loop or open-loop system. The following is assumed.

Assumption 1 The dynamic process $J(z) \in \mathcal{RH}_\infty$ with $J(z)$ strictly proper, i.e., $\lim_{z \to \infty} J(z) = 0$.

The disturbance $v$ is periodic with period $N$ according to

$$v(k + N) = v(k) \forall k. \quad (3)$$

The internal model principle (IMP) [5] states that an internal model of the disturbance has to be included in a feedback controller to asymptotically reject the influence of the disturbance on the dynamic process, i.e.,

$$\lim_{k \to \infty} e(k) = 0. \quad (4)$$

The structure of a typical RC is depicted in Fig. 2. In this RC, the internal model is formed by a buffer with length $N$ in positive feedback interconnection with itself, complemented by learning filter $L$ and robustness filter $Q$ according to

$$\frac{u(z)}{e(z)} = R(z) = \frac{LQz^{-N}}{1 - Qz^{-N}}, \quad (5)$$

where $z^{-N}$ represents the buffer, and $z^{-N} + L, z^{-N}Q \in \mathcal{RH}_\infty$, with finite preview $n_L, n_Q \in \mathbb{Z}_{\geq 0}$.

A large class of repetitive controllers can be designed in the frequency domain using non-parametric models, more specifically, using identified FRF data. The repetitive controller of Fig. 2 is stable for all buffer lengths $N$ if

$$\sup_{\omega \in [0, \pi]} |(1 - J(e^{j\omega})L(e^{j\omega}))Q(e^{j\omega})| < 1, \quad (6)$$

see [1]. The above criterion can directly be verified using non-parametric FRF data for $J(e^{j\omega})$. Consequently, $L$ is designed as an (approximate) inverse of $J$ for stability. $Q$ is designed as a low-pass filter to prevent learning instability for high frequencies due to mismatch of the plant inverse. Multiple methods exist for designing the approximate inverse $L$, such as ZPETC [18] or preview control [19]. $Q$ is usually designed as a zero-phase finite impulse response filter [1].

In this traditional setting, it is assumed that error information is available at each timestep $k$. There exists a well established RC framework to reject the disturbance $v$ based on this equidistant error data.

B. The Timestamping Operator

In many control applications, a measurement of $e(k)$ is not available at each timestep, but the time instance of the measurement, i.e., its timestamp, is available, resulting in non-equidistant but exact measurement data. This can be modelled by a timestamping operator that encodes the availability of information at each timestep. The timestamping operator is a memoryless, linear time-varying (LTV) system.

Definition 2 The timestamping operator $T$ outputs its input at the timestamps, and 0 otherwise, according to

$$T : e(k) \mapsto \bar{e}(k), \quad \bar{e}(k) = \begin{cases} e(k) & \text{if } k \in \Psi \\ 0 & \text{otherwise} \end{cases}, \quad (7)$$

in which $\Psi$ is a sequence of timestamps, unknown in advance but measurable during operation, according to

$$\Psi = \{\tilde{k}_1, \tilde{k}_2, \ldots\}, \quad \tilde{k}_i \in \mathbb{N}, \quad \tilde{k}_i < \tilde{k}_{i+1}, \quad (8)$$

where $\tilde{k}_i$ is the timestamp of measurement $i \in \mathbb{Z}_{\geq 0}$.

In the RC setting with a timestamping operator, only $\bar{e}(k)$ is available to reject periodic disturbances $v(k)$. To reject $v(k)$ in this setting, the intermittent sampling repetitive control setup in Fig. 1 (right) is considered. Two assumptions are made regarding the timestamping operator.

Assumption 3 The measurement of the error is exact at the timestamps, i.e., $e(k) = y(k) + v(k) \forall k \in \Psi$.

Assumption 4 The sequence of timestamps $\Psi$ is independent of the timestamping operator input $e$.

Assumption 3 defines the ideal timestamping operator. Assumption 4 allows for stability guarantees through a worst-case analysis, in which the sequence of timestamps $\Psi$ consists of arbitrary non-equidistant timestamps.

The timestamping operator can be used to model a variety of systems, e.g.,

1) optical encoders that output the exact position at line transitions [20], and

2) networked control systems subject to package loss.

Low-resolution optical encoders fit directly in this framework, since the measurement can be considered exact at the timestamps. High-resolution encoders require a high

Fig. 1. Traditional repetitive control setup (left) and intermittent sampling repetitive control setup (right) with periodic disturbance $v$ and timestamping operator $T$ resulting in the intermittently sampled error $\bar{e}$. Equidistant signals are indicated by full lines (---), intermittent signals are dotted (---).
sampling rate of the encoder output. This can be captured in the framework by exploiting frequency domain lifting techniques [21] to obtain a single-rate setting. The problem considered is the design of repetitive controllers for process $J$ using the intermittent error $\bar{e}$ from timestamping operator $\bar{T}$.

C. Problem Definition

The aim of this paper is to develop an intermittent sampling repetitive control framework to asymptotically reject the influence of $v(k)$ on dynamic process $J$ using intermittent samples $\bar{e}(k)$ from timestamping operator $\bar{T}$. This includes

1) developing frequency domain stability tests for arbitrary timestamp realizations $\Psi$ based on non-parametric FRF data analogous to (6) (Section III),
2) converting the stability test into a systematic frequency domain design framework that is similar to existing design frameworks (Section IV), and
3) validating the framework experimentally (Section V).

III. STABILITY OF THE INTERMITTENT SAMPLING REPETITIVE CONTROL SETUP

In this section, stability criteria for the intermittent sampling RC setup of Fig. 1, that can be validated using identified FRF data, are derived. First, the intermittent sampling RC setup is rewritten to the standard negative feedback interconnection of Fig. 4 (left). Secondly, two stability conditions are derived, constituting contribution C1.

A. The Timestamping Operator Complement

To derive stability results, the intermittent sampling RC setup is rewritten to the standard negative feedback interconnection of Fig. 4 (left), consisting of a discrete time LTI system $W$ and a memoryless function $\phi$. The intermittent error $\bar{e}(k)$ can be represented as the combination of the error of the traditional RC setup $e(k)$, and a mechanism that models the unavailability of data outside the timestamps, as opposed to the availability of data at the timestamps, see Fig. 3. The timestamping operator complement $\bar{T}$ is a memoryless, LTV operator that models the unavailability of data as defined below.

Definition 5 The timestamping operator complement $\bar{T}$ outputs $0$ at the timestamps, and its input otherwise, i.e.,

$$\bar{T} : e(k) \to \bar{e}(k), \bar{e}(k) = \begin{cases} 0 & \text{if } k \in \Psi \\ e(k) & \text{otherwise.} \end{cases}$$

such that $\bar{T}(k, e(k)) + \bar{T}(k, e(k)) = e(k)$.

Consequently, the intermittent error is given by

$$\bar{e}(k) = e(k) - \bar{T}(k, e(k)),$$

such that the intermittent sampling RC setup can be interpreted as a double feedback interconnection, see Fig. 3, in which the error $\bar{e}(k)$ consists of an LTI and equidistantly sampled contribution $e(k)$ and an additional LTV and non-equidistantly sampled contribution $\bar{T}(k, e(k))$.

Subsequently, the memoryless function $\bar{T}$ is isolated. This is possible due to linearity of the repetitive controller $R$ and dynamic process $J$. The input $\bar{e}(k)$ of the timestamping operator complement $\bar{T}$ is written as a function of its output $\bar{e}(k)$ and the exogenous signal $v(k)$, see Fig. 3, as

$$e(k) = T_R \bar{e}(k) + S_R v(k),$$

$$T_R = (1 + JR)^{-1} JR, S_R = (1 + JR)^{-1},$$

resulting in the negative feedback interconnection of $-T_R$ and $\bar{T}$ depicted in Fig. 4 (right). $T_R$ can be recognized as the complementary sensitivity of the RC loop in the traditional setting. As the timestamping operator complement is the only time-varying operator, the resulting systems $T_R, S_R$ are LTI.

The resulting interconnection fits in the standard negative feedback interconnection of Fig. 4 (left) with discrete time LTI system $W = -T_R$ and memoryless function $\phi = \bar{T}$, and enables the application of stability analysis based on dissipativity and small-gain theory, as investigated next.

B. Passivity-based Stability Analysis

In this section, stability of the intermittent sampling RC setup using passivity arguments is established, for a given RC design $R$ and based on identified FRF data of $J$. This constitutes contribution C1.

Consider again the standard negative feedback interconnection of Fig. 4 (left). The following result applies.

Lemma 6 The real rational transfer function $W(z) \in \mathcal{RH}_\infty$ is discrete positive real (DPR) if

1) $W(z)$ is analytic in $|z| \geq 1$, and
2) $W(e^{j\omega}) + W(e^{-j\omega}) = 2\Re(W(e^{j\omega})) \geq 0 \forall \omega \in [0, \pi]$.

Lemma 6 is a special case of Lemma 2 of [22], with $W$ SISO and $W \in \mathcal{RH}_\infty$. The following Lemma relates uniform stability of the standard negative feedback interconnection of Fig. 4 to a DPR condition on the transfer function $W$.

Lemma 7 Consider the negative feedback interconnection of $W$ and $\phi(k, w_2(k))$ in Fig. 4, where $W$ is strictly proper, and $\phi(k, w_2(k))$ is a memoryless function in the sector with boundaries $q_2 = 0$ and $q_2 = K^{-1}w_2$, $K \in \mathbb{R}_{>0}$, such that

$$\phi(k, 0) = 0,$$

$$\phi(k, w_2(k)) (K\phi(k, w_2(k)) - w_2(k)) \leq 0.$$


If \( K + W(z) \) is discrete positive real as in Lemma 6, the feedback system is globally uniformly stable [22].

The proof is based on a discrete time counterpart of the Kalman–Yakubovich–Popov Lemma. Lemma 7 is applied to the timestamping operator complement \( \hat{T} \).

**Lemma 8** The timestamping operator complement \( \hat{T} \) satisfies the sector bound conditions (12) with \( K = 1 \).  

Lemma 6, 7 and 8 allow for the following stability theorem for the intermittent sampling RC setup.

**Theorem 9** (Passivity-based stability analysis) Consider the intermittent sampling RC setup of Fig. 1 with \( J \in \mathcal{RH}_\infty \) and \( J \) strictly proper, periodic disturbance \( v \), and timestamping operator \( \hat{T} \). The repetitive controller \( R \) results in a uniformly stable feedback interconnection if

1. \( J(e^{j\omega})R(e^{j\omega}) \) does not encircle and does not intersect the point \( z = -1 \) for \( \omega \in [0, \pi] \), and
2. the negative complementary sensitivity \( -T_R(e^{j\omega}) = -\left(1 + J(e^{j\omega})R(e^{j\omega})\right)^{-1} J(e^{j\omega})R(e^{j\omega}) \) is confined to the region \( \mathcal{Y}_1 = \{ z \in \mathbb{C} | \Re(z) \geq -1 \} \) for \( \omega \in [0, \pi] \), see Fig. 5.

Theorem 9 is a two-fold stability theorem based on sequential loop-closing that can be validated using identified FRF data of \( J \). It consists of a Nyquist stability requirement S1 for the traditional RC loop based on equidistant error data, and a non-strict passivity requirement S2 as an additional condition imposed by the intermittent sampling characteristics.

**Example 10** For the typical RC of Fig. 2 with transfer function (5), the complementary sensitivity reads as

\[
T_r(z) = \frac{J(z)Q(z)z^{-N}}{1 - (1 - J(z)L(z))Q(z)z^{-N}}. \tag{13}
\]

Condition S1 of Theorem 9 is implied by the small-gain stability criterion (6) [1], such that \( T_R \in \mathcal{RH}_\infty \). For this RC structure, Condition S2 is given by

\[
\Re\left(\frac{J(e^{j\omega})L(e^{j\omega})Q(e^{j\omega})e^{-j\omega N}}{1 - (1 - J(e^{j\omega})L(e^{j\omega}))Q(e^{j\omega})e^{-j\omega N}}\right) \geq -1,
\tag{14}
\]

\( \forall \omega \in [0, \pi] \), such that the typical RC of Fig. 2 is stable in the intermittent sampling setting if (6) and (14) are satisfied.

**C. Small-gain Stability Analysis**

In this section, small-gain arguments are used to derive a sufficient test for asymptotic stability of the intermittent sampling RC setup, for a given RC design \( R \) and based on identified FRF data of \( J \). In contrast to the passivity based test, the small-gain test can be validated based as simple magnitude constraint on the complementary sensitivity \( T_R \), but introduces additional conservatism, see Fig. 5.

To employ small-gain arguments for stability, the worst-case energy gain of a system, i.e., its induced \( \ell_2 \)-gain, is defined.

**Definition 11** The induced \( \ell_2 \)-gain of a linear SISO system \( W \in \mathcal{RH}_\infty \) is given by

\[
\| W \|_{\ell_2,i} = \sup_{w_1 \in \ell_2, w_1 \neq 0} \frac{\| Ww_1 \|_{\ell_2}}{\| w_1 \|_{\ell_2}}. \tag{15}
\]

The worst-case energy gain can be used to infer stability of the standard negative feedback interconnection of a linear system \( W \) and memoryless function \( \phi \).

**Lemma 12** (Small-gain theorem) Consider the negative feedback interconnection of \( W \) and \( \phi(k, w_2(k)) \) in Fig. 4, where \( W \) is strictly proper and \( \phi(k, w_2(k)) \) is a memoryless function. If the loop gain \( W\phi \) satisfies

\[
\| W\phi \|_{\ell_2,i} < 1, \tag{16}
\]

then the feedback system is globally asymptotically stable.

See, e.g., [23] for a proof. Lemma 12 allows for the following stability theorem for the intermittent sampling RC setup.

**Theorem 13** (Small-gain stability analysis) Consider the intermittent sampling RC setup of Fig. 1 with \( J \in \mathcal{RH}_\infty \) and \( J \) strictly proper, periodic disturbance \( v \), and timestamping operator \( \hat{T} \). The repetitive controller \( R \) results in an asymptotically stable feedback interconnection if

1. \( J(e^{j\omega})R(e^{j\omega}) \) does not encircle and does not intersect the point \( z = -1 \) for \( \omega \in [0, \pi] \), and
2. the complementary sensitivity \( T_R(e^{j\omega}) = (1 + J(e^{j\omega})R(e^{j\omega}))^{-1} J(e^{j\omega})R(e^{j\omega}) \) is confined to the region \( \mathcal{Y}_2 = \{ z \in \mathbb{C} | \Re(z) < 1 \} \), i.e., \( |T_R(e^{j\omega})| < 1 \) for \( \omega \in [0, \pi] \) see Fig. 5.

Similar to Theorem 9, Theorem 13 is a two-fold stability test based on sequential loop-closing that can be validated using identified FRF data of \( J \), in which the second stability condition S2 is a small-gain condition on \( T_R \) as opposed to a discrete positive real condition on \( I - T_R \).

The stability definition of Theorem 13 differs from Theorem 9: for any timestamp realization \( \Psi \), asymptotic stability requires convergence, while the passivity argument just requires boundedness. In case no data is available, i.e., \( \hat{T} = 1 \) and \( \Psi = 0 \), asymptotic stability requires the internal model states, e.g., the buffer elements in the typical RC of Fig. 2, to converge. This corresponds to the difference in stability regions, see Fig. 5, i.e., the difference between the closed half space \( \mathcal{T}_1 \), which includes the point \( z = -1 \), and the open unit disk, which does not. In other words, Theorem 13 implies Theorem 9.

In conclusion, the small-gain based stability theorem is more intuitive stability condition that can be validated based on a simple magnitude constraint on \( T_R \), but it introduces conservatism with respect to Theorem 9.
IV. DESIGN ASPECTS

In this section, a design framework for intermittent sampling RC is presented that develops intuitive design guidelines to satisfy Theorem 9, constituting contribution C2.

The design procedure is two-fold. First, the repetitive controller is designed for stability of $T_R$ according to one of the methods in literature [1], [6], [14]. Second, the design is validated against the second condition of Theorem 9. The design is iterated until both conditions are satisfied. When iterating the design, the waterbed effect is often the limiting factor: a sufficiently high learning gain increases the magnitude of $-T_R(e^{j\omega})$ outside $\mathcal{T}_1$, i.e., left of the line $\Re(z) = -1$, around the cross-over frequency $\omega_0$ for which $|J(e^{j\omega_0})R(e^{j\omega_0})| = 1$.

The following procedure illustrates the design for the typical RC of Fig. 2.

**Procedure 14** (RC design for intermittent sampling)

1) Choose the appropriate RC type and determine $T_R$.
2) Design the RC such that it is stable in the non-intermittent setting, i.e., such that $T_R \in \mathcal{R}H_{\infty}$. For the typical RC of Fig. 2, this consists of the following three steps to satisfy (6).
   a) Obtain an approximate parametric model $\hat{J}$.
   b) Design $L$ as an approximation of $J^{-1}$ [19].
   c) Design $Q$ as a zero-phase finite impulse response low-pass filter such that $Q(e^{j\omega}) = 1$ at frequencies where $|1 - J(e^{j\omega})L(e^{j\omega})| \ll 1$ for learning performance, and $Q(e^{j\omega}) \ll 1$ at frequencies where $|1 - J(e^{j\omega})L(e^{j\omega})| \geq 1$ for stability.
3) Modify the design for the non-intermittent setting such that $S_2$ of Theorem 9 is satisfied, i.e., such that $-T_R(e^{j\omega}) \in \mathcal{T}_1$, by decreasing the magnitude response of $T_R(e^{j\omega})$ around the cross-over frequency $\omega_0$.
   a) Scale $L$ as $\alpha L$, $\alpha \in [0, 1] \subset \mathbb{R}$, and decrease $\alpha$.
   b) Decrease the magnitude of $Q$ locally around $\Omega = \{\omega \mid \Re(-T_R(e^{j\omega})) < -1\}$.

Both design heuristics in the third step guarantee stability of the RC in the intermittent sampling framework. The first heuristic slows down learning but does not limit the converged learning performance, and is thus preferred over the second, which limits the converged learning performance for frequencies $\omega \in \Omega$, but does not slow down learning.

This design procedure can be applied to other RC types, like MBFRC [14], by adhering to the non-intermittent design guidelines for that type in the second step. In the third step, design heuristic 3a can be applied to every RC type.

V. EXPERIMENTAL RESULTS

In this section, the developed RC framework is validated on an industrial printbelt system (contribution C3).

A. Setup

The framework is illustrated using a printbelt module similar to the one in the Canon Varioprint i300 [24]. In this printer, paper sheets are transported underneath an inkjet printing station by a printbelt, which is guided along a set of rollers. The belt is actuated by a voltage-driven motor at 500 Hz. The position of the paper is measured by means of a perforated belt edge and optical sensors. This printbelt setup, in continuous operation with constant velocity, fits in the intermittent sampling framework of Fig. 1 (right), as the distance between the holes in the belt is large, such that measurements of the belt position are intermittent and can be considered exact at the timestamps. The Bode diagram of the transfer from motor input to belt position (pre-stabilized by feedback on another sensor) is shown in Fig. 6. Note that advanced system identification techniques are necessary due to the intermittent sampling characteristics [25].

B. Experimental Results

The main disturbance is caused by the drivetrain dynamics and eccentricity with a period that is a non-integer amount of samples. Consequently, a matched basis functions repetitive controller (MBFRC) [14] is designed to reject this disturbance. The MBFRC is designed such that the conditions in Theorem 9 are satisfied based on the identified FRF data of $J$ without obtaining a parametric model, guaranteeing stability of the intermittently sampled repetitive control setup.

Fig. 7 shows the learning curve of the repetitive controller. The MBFRC is able to reduce the $\text{RMS}$-norm of the error by a factor 7 based on only the intermittently sampled non-equidistant error, as compared to a situation without RC.

Fig. 8 and 9 show the initial and converged error in time and frequency domain respectively. The MBFRC reduces the maximum absolute error by a factor 4 compared to a situation without RC, based on non-equidistant and trial-variant error data. Furthermore, the amplitude of the error at the drivetrain disturbance frequency of 3.5 Hz is reduced by a factor 10.

VI. CONCLUSION

In this paper, a repetitive control framework is introduced that directly enables implementation of RC for a broad
of the intermittent sampling MBFRC design, constructed
initial error (•) and converged (●) error are shown in
Fig. 8 and 9.

Fig. 8. Converged error of the intermittent sampling MBFRC design
compared to the initial error. The error at the timestamps is given by
(●) and (○) respectively. The linear interpolation of the error is shown in
(•), and the maximum and minimum value of the error in (○), both in
their respective color. The maximum absolute error is reduced by a factor
4. Observe that the available error data is non-equidistant in time (inset).
Furthermore, the time instances of the available error data are trial-variant.

Fig. 9. Cumulative amplitude spectrum of the converged error (●) and
initial error (○) of the intermittent sampling MBFRC design, constructed
from the linearly interpolated equidistant error. The amplitude of the
disturbance associated with the drivetrain at 3.5 Hz is reduced by a factor
10 by the MBFRC design.

range of applications with intermittent sampling characteristics,
such as systems that employ optical encoders and
networked systems with package loss. Stability conditions
are derived for any measurement realization based on small-
gain and passivity analysis. The conditions are converted into
a straightforward design framework based on loop-shaping
and identified FRF data that explicitly allows for addressing
uncertainty, closely resembling common RC applications for
non-intermittent sampling. The RC framework is experi-
mentally validated through implementation on an industrial
printbelt system at Canon Production Printing.

REFERENCES

systems,” European Journal of Control, vol. 16, no. 5, pp. 447 – 496,
2010.
learning control,” IEEE Control Systems Magazine, vol. 26, no. 3,
[3] R. W. Longman, Designing Iterative Learning and Repetitive Con-
control: Decentralized designs with application to continuous media
flow printing,” IEEE/ASME Transactions on Mechatronics, vol. 25,
engineering practice,” International Journal of Control, vol. 73, no. 10,
of four discrete-time repetitive control algorithms,” IEEE Control
of Discrete-Time Repetitive Controllers,” Journal of Dynamic Systems,
system: a new type servo system for periodic exogenous signals,” IEEE
[10] M. Steinbuch, “Repetitive control for systems with uncertain period-
time robust high-order repetitive control, with application to optical
multiperiod repetitive control design with application to industrial
wide-format printing,” IEEE/ASME Transactions on Mechatronics,
control system for multiple periods,” in Proceedings of the 39th IEEE
ory for matched basis function repetitive control,” Acta Astronautica,
vol. 95, pp. 260–271, 02 2014.
[15] N. Strijbosch and T. Oomen, “Intermittent sampling in iterative learn-
ing control: a monotonically-convergent gradient-descent approach
with application to time stamping,” in 2019 IEEE 58th Conference
on Decision and Control (CDC). United States: Institute of Electrical
and Electronics Engineers, 2019, pp. 6542–6547.
iterative learning controller with independent data dropouts,” IFAC
IFAC World Congress.
[17] D. Shen and Y. Wang, “Iterative learning control for networked
stochastic systems with random packet losses,” International Journal
Control,” Journal of Dynamic Systems, Measurement, and Control,
[20] N. Strijbosch and T. Oomen, “Beyond quantization in iterative learn-
ing control: Exploiting time-varying time-stamps,” in Proc. of the 2019
improving intersample behavior in iterative learning control,” in 2021
[22] L. Hitz and B. D. O. Anderson, “Discrete positive-real functions and
their application to system stability,” Proceedings of the Institution
Systems: Input–Output Properties, C. A. Desoer and M. Vidyasagar,
[24] Canon Production Printing Vento. VarioPrint i300. [Online]. Avail-
able: https://www.canon-europe.com/business-printers-and-faxes/cut-
sheet-colour-printers/varioprint-i300
ar processes from unevenly sampled data,” Automatica, vol. 38, no. 4,